

PRINCIPAL COMPONENT ANALYSIS AND THERMOMECHANICAL PREFERENCE OF WHITE Au ALLOYS WITHOUT Ag

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ABSTRACT. Addition of different amounts of Cu and Ag to Au alloys, as well as some new elements (Zn and Cd), gives alloys of the different colour spectrum (from red to yellow) and different technological and metallurgical characteristics. The trend today is the implementation of new alloys not containing Ag, and including new elements, such as Ga and In. Differences in two Au alloys exist: the first alloy contains Ni and Pd, and the second alloy is without them. The values of electrical conductivity and hardness are different, due to the reduction, which was shown using PCA ($r=0.985$ and the strong positive correlation between hardness and electrical conductivity). Performed tests confirm that those multiphase multi component gold alloys can find their application not only in jewellery making but also in the world of modern electrical engineering. The performed statistical analysis shows strong positive and negative correlations of properties of investigated Au alloys, and it provides significant savings in the design and efficiency of metallurgical processes.

Keywords: alloy, PCA, metallurgical process.

INTRODUCTION

The subject of this work, through the prism of processing metallurgy and legal metrology, was to determine the conditions for obtaining semi-finished products in jewellery with a suitable equivalent axial structure (with

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the crystal grains of the same crystallographic orientation, and the grains about the same shape and boundaries), and optimal physico-chemical and mechanical properties. Our first aim, in the framework of this task, was to obtain multi-component alloys of gold and white colours for melting and casting and then investigate their formation in the solid state. The method of cold rolling of the molded pieces in combination with certain annealing processes gives plastic properties for the material that are optimal for cold rolling and drawing, as well as further cold deformations of samples.

The latest medical and technological achievements led us to focus, in this paper, on so far poorly investigated 585 alloys of gold for white jewellery, without Ag, mostly in the form of annealed and cold-deformed sheet, strip, tube and wire [1,2]. The investigated gold alloys are of quantitative composition Au₅₈₅Cu₃₁₂Zn₄₀Ga₃₅In₂₈ (white and reddish-gray colour) and Au₅₈₅Cu₂₃₃Ni₈₀Zn₇₀Pd₃₂ (white-gray colour).

Regarding applied statistical analysis tool, we used non-parametric analysis - principal component analysis (PCA) in order to obtain the initial solution reducing the original dataset [3-5]. The earliest works in principal component analysis can be found in Karl Pearson (1901) [6]. In chemistry, PCA was firstly introduced by Malinowski in 1960s as a principal factor analysis [7].

In this work, we used microstructural analysis, metallography with optical microscopy and scanning electron microscopy (SEM) with energy-dispersive spectroscopy (EDS) in combination with principal component analysis (PCA), and contributed to better understanding of new Au alloys.

RESULTS AND DISCUSSION

A cold-rolled sheet of alloy Au₅₈₅Cu₂₃₃Ni₈₀Zn₇₀Pd₃₂ (thickness 0.38 mm and hardness HV 155) was examined by straining [8-10]. The obtained value was $R_m = 610$ MPa, and the relative elongation $A_{100} = 35$ %. The hardness of samples increases monotonically from 155 HV in a molten state, up to 316 HV after 8 reductions in rolling mills, with the total degree of deformation increasing up to 71.74 % (Table 1). After the first annealing hardness decreases to 183 HV, and with subsequent cold deformation, after 3 reductions in rolling mills, increases monotonically up to 314 HV with the increase of the degree of cold deformation to 91.74 %. After the second annealing, the hardness of the sample decreases to 160 HV with the increase of the degree of cold deformation to 70.70 % [11-13].

PCA performs reductions of data matrix by transforming the data into orthogonal components (F1-F4) that represent a linear combination of the original variables (samples I-XII from Table 1). Before applying PCA analysis, we tested the data matrix in order to detect outliers. Application of Grubb's

test to experimental data resulted in the detection of no outliers in the datasets (the critical value for $\alpha=0.05$ and $n=12$ was 2.412). Strong positive correlations were observed between data of Width (b) and Hardness (HV10) ($r=0.833$), Width (b) and Electrical conductivity (MS/m) ($r=0.823$), and Hardness (HV10) and Electrical conductivity (MS/m) ($r=0.989$); and strong negative correlations between Width (b) and Height (h) ($r=-0.980$), Height (h) and Hardness (HV10) ($r=-0.887$), and Height (h) and Electrical conductivity (MS/m) ($r=-0.867$) [14,15]. From the shape of the scree plot, shown in Fig. 1a, the number of important components that will be used in further calculations can be observed.

Table 1. The ratio of elongation, hardness and electrical conductivity for the alloy Au585Cu233Ni80Zn70Pd32, depending on the degree of reduction

Sample	Width (b) (mm)	Height (h)(mm)	ϵ total	ϵ individually	F ₀ /F	Hardness (HV 10)	Electrical conductivity (MS/m)
I	28.3	4.6				155	5.83
II	28.4	4.4	4.35%	4.35%	1.0454	162	5.86
III	28.6	4.1	10.87%	6.81%	1.1219	174	5.88
IV	28.7	3.6	21.74%	12.19%	1.2778	209	5.91
V	28.8	3.1	32.61%	13.89%	1.4839	244	5.97
VI	29.0	2.7	41.30%	12.90%	1.7037	263	6.00
VII	29.1	2.2	52.17%	18.52%	2.0909	276	6.03
VIII	29.2	1.7	63.04%	22.73%	2.7058	298	6.08
IX	29.4	1.3	71.74%/0%	23.53%	3.5385	316/183 ^A	6.12/5.89 ^A
X	29.6	0.86	81.30%/33.85%	33.85%	5.3489	247 ^B	5.96
XI	29.9	0.58	87.39%/55.38%	32.56%	7.9310	280	6.05
XII	30.1	0.38	91.74%/70.70%	34.48%	12.1053	314/160 ^A	6.11/5.85 ^A

^A values after annealing, T = 650°C, t = 10 min.

^B sample was taken for wire making.

PCA of dataset revealed the presence of one component with characteristic value (3.690) exceeding 1, explaining 92.249 % of the variability. Based on the Kaiser criterion [16], two components (F1 and F2) will be used in further explanations of variances. This two-component solution explained a total of 99.354 % of the variance, with the contribution of the first component of 92.249 %, and the second component of 7.105 %. Since two-component solution based on the Kaiser criterion explained 99.354 % of the total variability, this criterion was accepted. Observation plot based on the contents of components is represented in Fig. 2a.

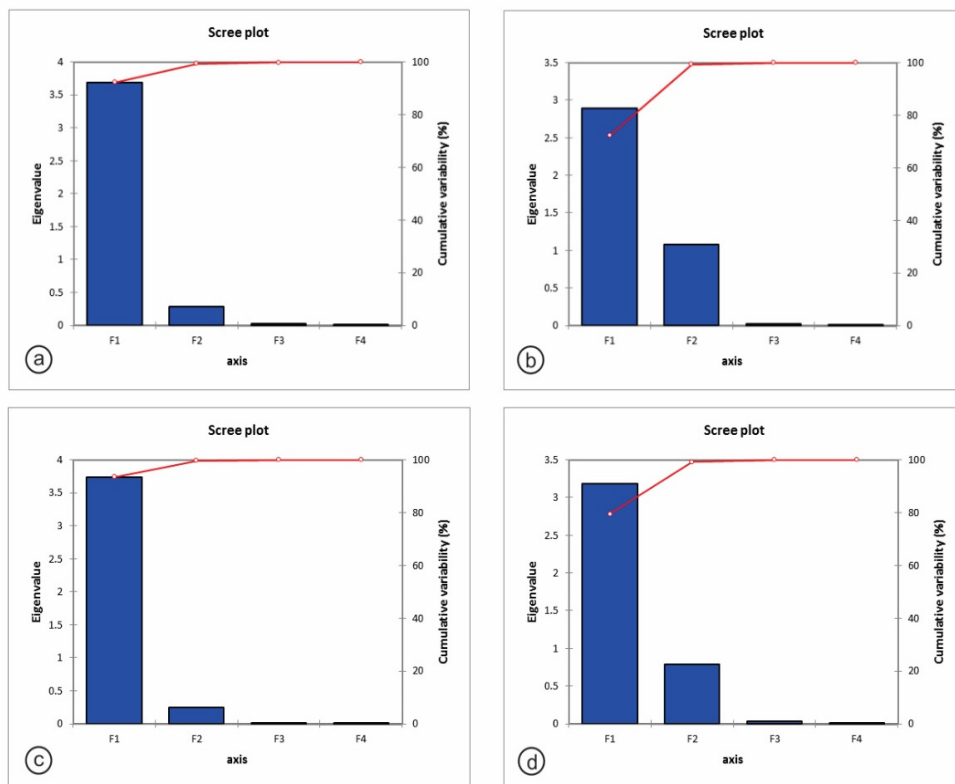


Figure 1. Scree plots of Eigen values

The high value of Width (b) is present in samples on the right side of the plot and low on the left side of the plot. Also, it can be concluded that high value of Height (h) is present in samples in the upper half of the plot and low on the opposite side of the plot (Fig. 2a).

The hardness of samples increases from 174 HV after forming the tube and welding, to 248 HV after 4 drawings at a tow bench and with increasing of the total coefficient of elongation to 1.1133 (Table 2). After interphase annealing hardness decreases to 181 HV, and with subsequent cold deformation after 3 drawings on the tow bench increases to 241 HV, with the increase of total coefficient of elongation to 1.406612 [11-13,17,18]. The cold-rolled sheet of alloy Au585Cu312Zn40Ga35In28 with the hardness of HV 150 of thickness 0.38 mm was examined by straining [8-10]. The obtained value is $R_m = 590$ MPa, while the relative elongation is $A_{100} = 34$ %. Before applying PCA analysis on the dataset, we examined the data matrix in order to detect outliers. Application of Grubb's test to experimental data resulted in the detection of no outliers in

Table 2. The ratio of elongation and hardness for a tube of alloy Au585Cu233Ni80Zn70Pd32, depending on the reduction degree

Sample	Length (l) (mm)	Diameter (Ø) (mm)	λ individually	λ total	Hardness (HV 10)	Electrical conductivity (MS/m)
I	150	6.0			174	5.88
II	152	5.8	1.0133	1.0133	187	5.90
III	157	5.6	1.0328	1.0466	208	5.92
IV	163	5.2	1.0382	1.0866	230	5.94
V	167	4.8	1.0245	1.1133	248/181 ^A	5.96/5.89
VI	180	4.6	1.0778	1.2000	200	5.90
VII	193	4.3	1.0722	1.2866	210	5.91
VIII	211	3.9	1.0932	1.4066	241	5.93

^A hardness of tubes after annealing

the datasets (the critical value for $\alpha=0.05$ and $n=8$ was 2.127). Strong positive correlations were observed between Hardness (HV10) and Electrical conductivity (MS/m) ($r=0.947$); and strong negative correlations between Length (l) and Diameter (Ø) ($r=-0.980$) [14,15]. From the shape of the scree plot, shown in Fig. 1b, the number of important components that will be used in further calculations can be observed (F1 and F2). PCA of dataset revealed the presence of two components with characteristic values (2.890 and 1.082) exceeding 1, explaining 99.282 % of variability. Based on the Kaiser criterion [16], two components will be used in further explanations of variances. This two-component solution explained a total of 99.282 % of the variance, with the contribution of the first component of 72.244 %, and the second component of 27.038 %. Since two-component solution based on the Kaiser criterion explained 99.282 % of the total variability, this criterion was accepted. Observation plot based on the contents of components is represented in Fig. 2b. The high value of Length (l) is present in samples on the right side of the plot and low on the left side of the plot. Also, it can be concluded that high value of Diameter (Ø) is present in samples in the upper half of the plot and low on the opposite side of the plot (Fig. 2b). The hardness of samples increases from 150 HV in a molten state, up to 310 HV after 7 reductions in rolling mills while the total degree of deformation increased to 73.91% (Table 3).

After the first annealing, hardness decreases to 180 HV, and with subsequent cold deformation, after 3 reductions in rolling mills increases to 305 HV with the degree of cold deformation increasing to 91.74%. After the second annealing, the hardness of samples decreases to 150 HV with increasing degree of cold deformation to 68.33% [8-10]. Application of Grubb's test for

the detection of outliers to experimental data (samples I-XI from Table 3) resulted in the detection of no outliers in the datasets (the critical value for $\alpha=0.05$ and $n=11$ was 2.355). Strong positive correlations were observed between data of Width (b) and Hardness (HV10) ($r=0.891$), Width (b) and Electrical conductivity (MS/m) ($r=0.843$), and Hardness (HV10) and Electrical conductivity (MS/m) ($r=0.985$); and strong negative correlations between Width (b) and Height (h) ($r=-0.994$), Height (h) and Hardness (HV10) ($r=-0.905$), and Height (h) and Electrical conductivity (MS/m) ($r=-0.854$) [14,15].

Table 3. The ratio of elongation, hardness and electrical conductivity of alloy Au585Cu312Zn40Ga35In28, depending on the reduction degree

Sample	Width (b) (mm)	Height (h) (mm)	ϵ_{total}	$\epsilon_{individually}$	F ₀ /F	Hardness (HV 10)	Electrical conductivity (MS/m)
I	28.6	4.6				150	5.80
II	28.7	4.3	6.52%	6.52%	1.0697	156	5.82
III	28.9	3.9	15.22%	9.30%	1.1795	172	5.87
IV	29.1	3.4	26.09%	12.82%	1.3529	204	5.90
V	29.3	2.7	41.30%	20.59%	1.7037	243	5.94
VI	29.6	2.1	54.35%	22.22%	2.1905	268	6.01
VII	29.8	1.6	65.22%	23.81%	2.8750	290	6.06
VIII	29.9	1.2	73.91%/0%	25.00%	3.8333	310/180 ^A	6.11/5.88
IX	30.1	0.8	82.61%/33.33%	33.33%	5.7500	240 ^B	5.93
X	30.3	0.5	89.13%/58.33%	37.50%	9.2000	275	6.02
XI	30.5	0.38	91.74%/68.33%	24.00%	12.1052	305/150 ^A	6.07/5.81 ^B

^A values after annealing, temperature 650°C, t = 10 min.

^B sample was taken for wire making.

From the shape of the scree plot, shown in Fig. 1c, the number of important components that will be used in further calculations can be observed (F1 and F2). PCA of dataset revealed the presence of one component with characteristic value (3.736) exceeding 1, explaining 93.4 % of the variability. Based on the Kaiser criterion [16], two components will be used in further explanations of variances. This two-component solution explained a total of 99.619 % of the variance, with the contribution of the first component of 93.4 %, and the second component of 6.218 %. Since two-component solution based on the Kaiser criterion explained 99.619 % of the total variability, this criterion was accepted. Observation plot based on the contents of components is represented in Fig. 2c.

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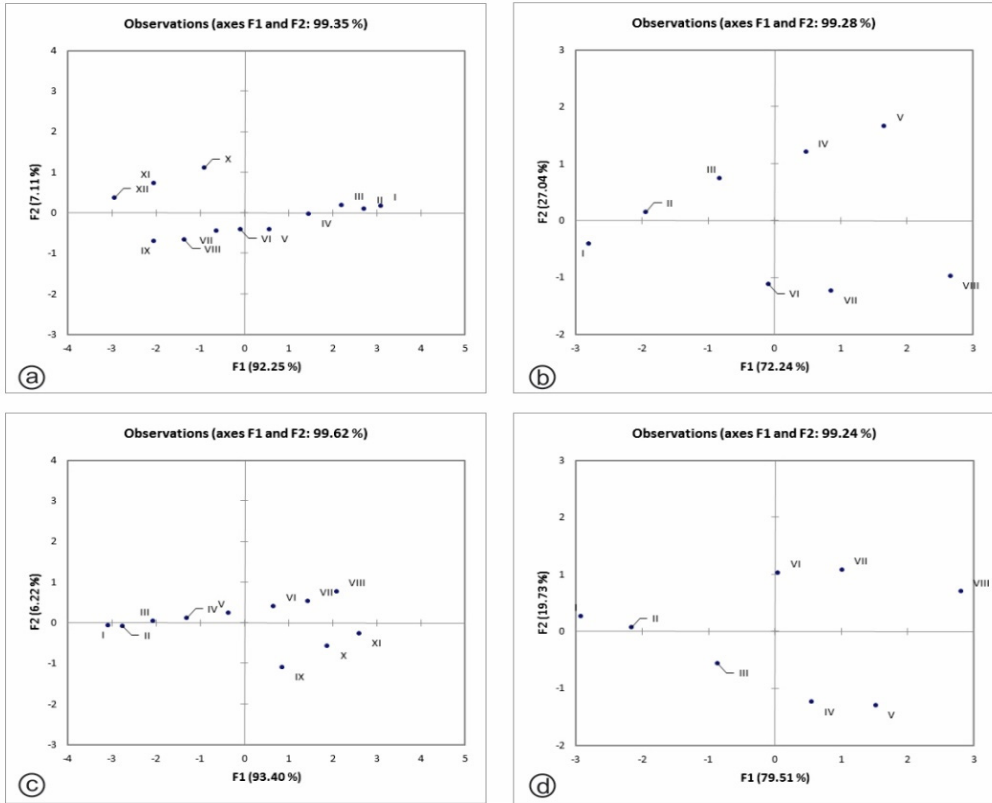


Figure 2. Principal component score plots (F1 and F2) of the studied samples

The high value of Width (b) is present in samples on the right side of the plot and low on the left side of the plot (Fig. 2c). Also, it can be concluded that high value of Height (h) is present in samples in the upper half of the plot and low on the opposite side of the plot.

The hardness of samples increases from 170 HV after forming the pipe and welding, up to 240 HV after 4 drawings at a tow bench with the increase of the total coefficient of elongation to 1.1400 (Table 4). After the interphase annealing hardness decreases to 171 HV, and with subsequent cold deformation after 3 drawings on the tow bench increases to 238 HV with the increase of the total coefficient of elongation to 1.4266 [8-10].

Application of Grubb's test to experimental data (samples I-VIII from Table 4) resulted in the detection of no outliers in the datasets (the critical value for $\alpha=0.05$ and $n=8$ was 2.127). Strong positive correlations were observed

between data of Hardness (HV10) and Electrical conductivity (MS/m) ($r=0.988$); and strong negative correlations between Length (l) and Diameter (\emptyset) ($r=-0.958$), and Hardness (HV10) and Diameter (\emptyset) ($r=-0.715$) [14, 15].

Table 4. The ratio of elongation and hardness of alloy Au585Cu312Zn40Ga35In28 tube depending on the reduction degree

Sample	Length (l) (mm)	Diameter (\emptyset) (mm)	λ individually	λ total	Hardness (HV 10)	Electrical conductivity (MS/m)
I	150	6.0			170	5.87
II	153	5.7	1.0200	1.0200	180	5.88
III	158	5.4	1.0326	1.0533	202	5.90
IV	164	5.1	1.0379	1.0933	228	5.92
V	171	4.7	1.0426	1.1400	240/171 ^A	5.93/5.88
VI	183	4.5	1.0701	1.2200	198	5.89
VII	195	4.2	1.0655	1.3000	208	5.90
VIII	214	3.9	1.0974	1.4266	238	5.92

^A hardness of tubes after annealing

From the shape of the scree plot, shown in Fig. 1d, the number of important components that will be used in further calculations can be observed (F1 and F2). PCA of dataset revealed the presence of one component with characteristic value (3.181) exceeding 1, explaining 79.513 % of the variability. Based on the Kaiser criterion [16], two components will be used in further explanations of variances. This two-component solution explained a total of 99.244 % of the variance, with the contribution of the first component of 79.513 %, and the second component of 19.731 %. Since two-component solution based on the Kaiser criterion explained 99.244 % of the total variability, this criterion was accepted. Observation plot based on the contents of components is represented in Fig. 2d. The high value of Length (l) is present in samples on the right side of the plot and low on the left side of the plot (Fig. 2d). Also, it can be concluded that high value of Diameter (\emptyset) is present in samples in the upper half of the plot and low on the opposite side of the plot.

The microstructure of cold-rolled sample of alloy Au585Cu233Ni80Zn70Pd32 (the overall reduction degree 71.74 %, the hardness of HV 316), was etched in the solution 10 % KCN: 10 % (NH₄)₂S₂O₈ in the ratio of 1:1 for 2 h at 40 °C, at 200 × magnification. Because of technological and metallurgical characteristics that are reflected in the higher hardness values, this sample is reduced 8 times at the rolling stands. The grains are elongated and oriented in the direction of the deformation (Figure 3a) [8-10, 13].

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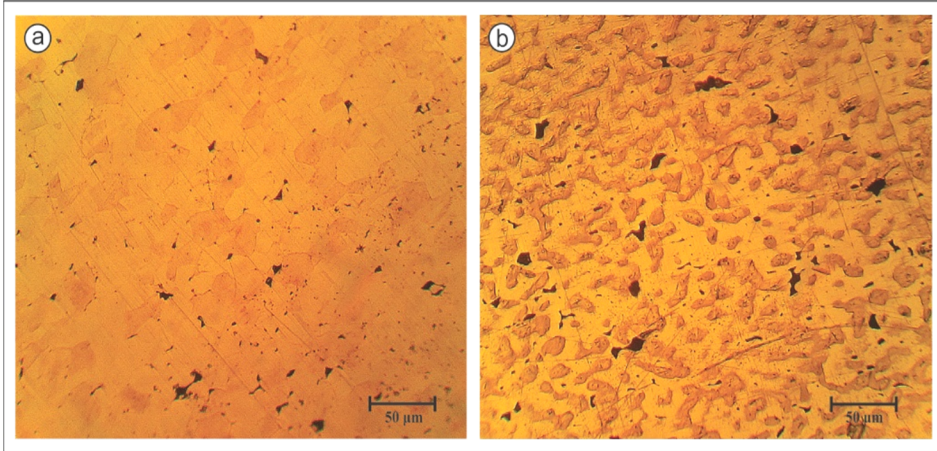


Figure 3. The pattern of alloy Au585Cu233Ni80Zn70Pd32 a) after 8 reductions of hardness HV 316, $\epsilon=71.74\%$ etched in the solution of 10 % KCN: 10 % $(\text{NH}_4)_2\text{S}_2\text{O}_8$ in the ratio of 1:1 for 2 h at 40 °C, at 200 x magnification, b) etched in the solution of 8 ml of distilled H_2O , 3 ml of HCl and HNO_3 in 1 ml where 2 g CrO_2 was added

The microstructure of annealed samples of white gold with nickel obtained by SEM method, magnified 500 times, where the points 2, 4 and 5, residing in the light phase, have less copper than the points 1 and 3, residing in the darker phase (Figure 4). Two distinct phases coexist, where the lighter contains a higher percentage of gold and a small percentage of copper, while the darker contains a lower percentage of gold and a higher percentage of copper.

Figure 5a shows the microstructure of cold-rolled sample with the overall reduction degree of 74.47%. The sample was reduced 7 times at the rolling stands, and a sample of white gold without nickel shows hardness values lower than the white gold alloy with nickel [8-10,13,19]. The grains are elongated and oriented in the direction of the deformation. There is also the occurrence of twin crystals and phases [12]. Figure 5b shows the sample from Figure 6a, which is annealed at a constant temperature of 923 K (650 °C) for 10 min. It can be observed the recrystallised structure of the multi-component system that is ready for further deformation [12].

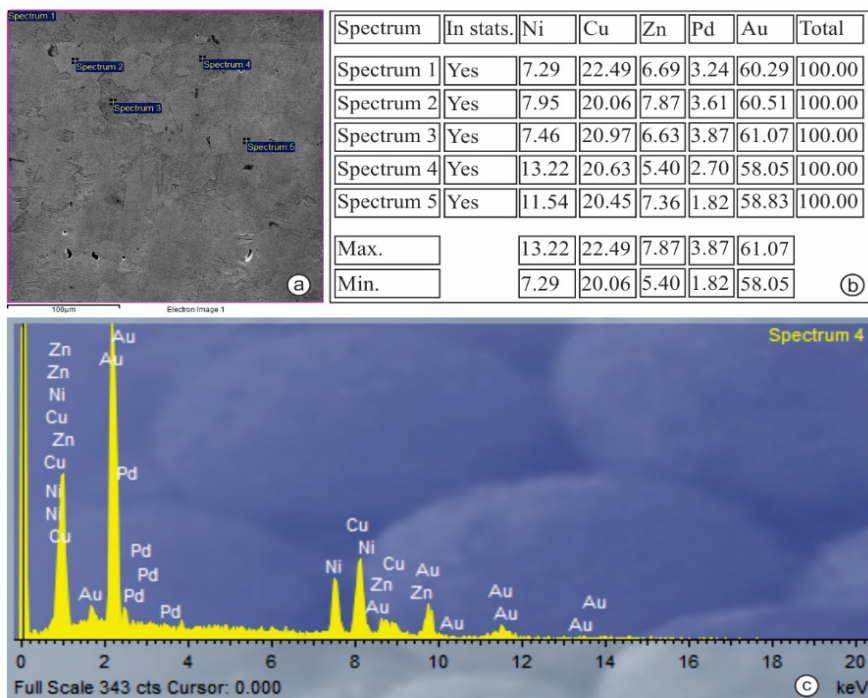


Figure 4. The microstructure of annealed samples of white gold with nickel: a) Overview of points for chemical composition analysis, magnification 500 \times , b) the table showing the content of the alloy components in the individual points, c) EDS spectrum analysis of point 4

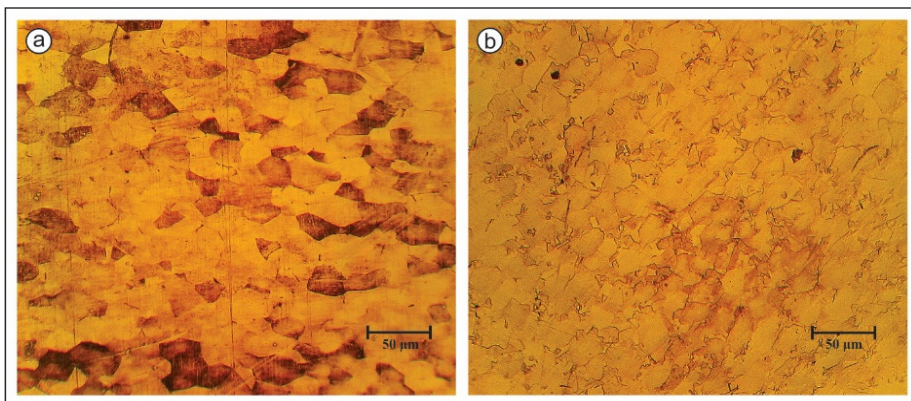


Figure 5. Pattern of alloy Au585Cu312Zn40Ga35In28 etched in KCN solution of 10%:10% $(\text{NH}_4)_2\text{S}_2\text{O}_8$ in the ratio of 1:1 for 2 hours at 40 °C, 200 \times magnification: a) after 7 reduction of hardness HV 313, $\epsilon = 74.47\%$, b) after the first annealing with hardness HV 180

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Figure 6 shows the microstructure of annealed recrystallised samples of the Au585Cu312Zn40Ga35In28 alloy obtained by SEM method with a magnification of 500 times, where it can be seen that points 1 and 2, from the lighter phase, have much less copper content than points 3 and 4, from the darker phase. Two different phases coexist, where the lighter one contains greater % of gold and lower % of copper, while the dark has lower % of gold and higher % of copper.

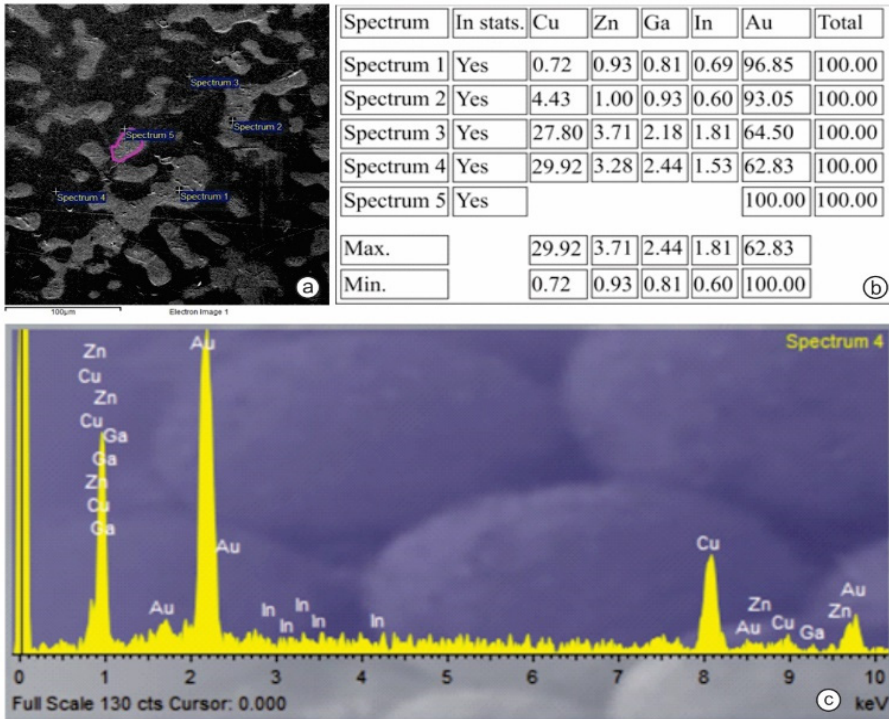


Figure 6. The microstructure of annealed recrystallised samples of Au585Cu312Zn40Ga35In28: a) Overview of points for chemical composition analysis, magnification 500×, b) the table shows the content of the alloy components in the individual points, c) EDS spectrum analysis of point 4

CONCLUSIONS

By rolling cast pieces of the white gold alloy without silver, high-quality rectangular profiles of flat-sheet-strips with smooth edges, without cracks, uniform thickness and width all along the length, were obtained. Using the method of

cold rolling, with the increase in the total strain, the curves for the hardness value show the increase for both types of samples, more for the alloy Au585Cu233Ni80Zn70Pd32 than for the alloy Au585Cu312Zn40Ga35In28. The values obtained for the tensile strength in both tested alloys are at the upper limit of the literature values, while the relative elongation values are in the field of expected values. The values of electrical conductivity and hardness are different, due to the reduction, which was shown using PCA ($r=0.985$ and the strong positive correlation between hardness and electrical conductivity). Annealing under these conditions does not achieve the desired recrystallised structure. It is concluded that it is necessary for this white gold alloy to be annealed for a longer period or at a higher temperature. The microstructure of this alloy type, analyzed by optical and scanning electron microscopy - SEM, shows that during the metallurgical processes, micro-structural changes of structures happened. The processes of crystal grains fragmentation play an important role in the grain boundary dislocations, impurities, and intermetallic compounds.

EXPERIMENTAL SECTION

Sample preparation was performed in an induction furnace graphite ladle (the processes of heating, melting, mixing and production). The resulting mixture was discharged into the wax-coated molds and casts of dimensions: 92 mm × 28.6 mm × 4.6 mm (Au585Cu312Zn40Ga35In28) and 92 mm × 28.3 mm × 4.6 mm (Au585Cu233Ni80Zn70Pd32). The resulting cast was several times on rolling stands (after every 5 passes it was annealed-recrystallised at 650 °C for 10 min) to achieve the appropriate sheet thickness-0.38 mm, which was suitable for cutting using circular shears.

Obtained strip (thickness 0.38 mm and a width 18.5 mm) was passed through the device for resistance welding in the presence of argon. The entire scheme of sampling is shown in Figures 7a and 7b.

Qualitative determination of the composition of the examined alloys using XRF device was performed in the Laboratory of the Directorate of Measures and Precious Metals in Belgrade, Republic of Serbia. Several investigations (hardness testing of samples, tensile testing, metallographic investigations, investigations using scanning electron microscopy and energy-dispersive spectroscopy, determination of electrical conductivity and determination of the colour of tested alloys) were conducted in the Laboratories of the Technical Faculty in Bor, Republic of Serbia [20-26].

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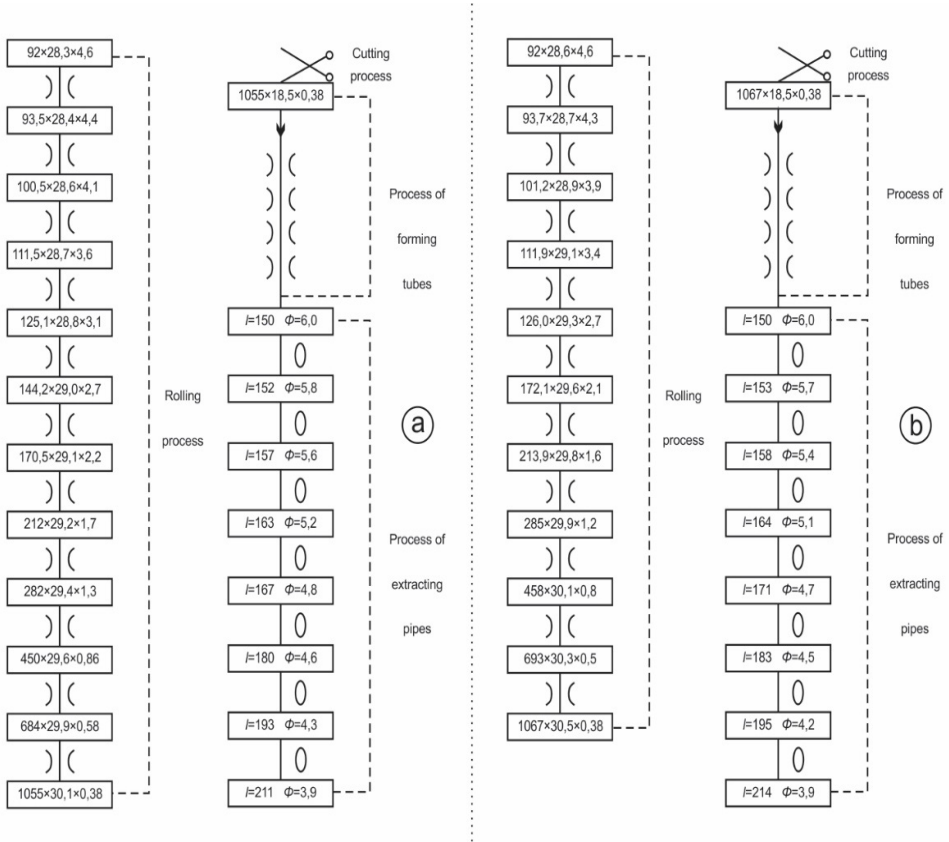


Figure 7. a) Pass plan for the alloys Au585Cu233Ni80Zn70Pd32, b) Au585Cu312Zn40Ga35In28

Statistical analysis (Principal component analysis)

The principal component analysis was used with the aim to evaluate the dataset, reducing its dimension and conserving most of the statistical information. PCA permits establishing the relationships among variables. The analysis was performed using statistical application available for Microsoft Excel® (XLSTAT 2015.6.01.24412, Addinsoft SARL, Paris, France) [27].

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